



Progression in Mathematics



Progression in Place Value

| COUNTING | | | | | | |
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| Reception | Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
| Count objects, actions and sounds Count beyond 10 Subitise. | count to and across 100, forwards and backwards, beginning with 0 or 1, or from any given number | | | count backwards through zero to include negative numbers | interpret negative numbers in context, count forwards and backwards with positive and negative whole numbers, including through zero | use negative numbers in context, and calculate intervals across zero |
| | count, read and write numbers to 100 in numerals; count in multiples of twos, fives and tens | count in steps of 2, 3, and 5 from 0, and in tens from any number, forward or backward | count from 0 in multiples of 4, 8, 50 and 100; | count in multiples of 6, 7, 9, 25 and 1000 | count forwards or backwards in steps of powers of 10 for any given number up to 1 000 000 | |
| | given a number, identify one more and one less | | find 10 or 100 more or less than a given number | find 1000 more or less than a given number | | |
| COMPARING NUMBERS | | | | | | |
| Understand the 'one more than/one less than' relationship between consecutive numbers | use the language of: equal to, more than, less than (fewer), most, least | compare and order numbers from 0 up to 100; use <, > and = signs | compare and order numbers up to 1000 | order and compare numbers beyond 1000 | read, write, order and compare numbers to at least 1 000 000 and determine the value of each digit (appears also in Reading and Writing Numbers) | read, write, order and compare numbers up to 10 000 000 and determine the value of each digit (appears also in Reading and Writing Numbers) |
| | | | | <i>compare numbers with the same number of decimal places up to two decimal places</i> | | |

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| | | | | (copied from Fractions) | | |
| IDENTIFYING, REPRESENTING AND ESTIMATING NUMBERS | | | | | | |
| | identify and represent numbers using objects and pictorial representations including the number line | identify, represent and estimate numbers using different representations, including the number line | identify, represent and estimate numbers using different representations | identify, represent and estimate numbers using different representations | | |

| READING AND WRITING NUMBERS (including Roman Numerals) | | | | | | |
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| Reception | Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
| | read and write numbers from 1 to 20 in numerals and words. | read and write numbers to at least 100 in numerals and in words | read and write numbers up to 1000 in numerals and in words | read Roman numerals to 100 (I to C) and know that over time, the numeral system changed to include the concept of zero and place value. | read, write, order and compare numbers to at least 1 000 000 and determine the value of each digit (appears also in Comparing Numbers) | read, write, order and compare numbers up to 10 000 000 and determine the value of each digit (appears also in Understanding Place Value) |
| | | | <i>tell and write the time from an analogue clock, including using Roman numerals from I to XII, and 12-hour and 24-hour clocks</i> (copied from Measurement) | | read Roman numerals to 1000 (M) and recognise years written in Roman numerals. | |
| UNDERSTANDING PLACE VALUE | | | | | | |
| | | recognise the place value of each digit in a two-digit number (tens, ones) | recognise the place value of each digit in a three-digit number (hundreds, tens, ones) | recognise the place value of each digit in a four-digit number (thousands, hundreds, tens, and ones) | read, write, order and compare numbers to at least 1 000 000 and determine the value of each digit (appears also in Reading) | read, write, order and compare numbers up to 10 000 000 and determine the value of each digit (appears also |

| NUMBER BONDS | | | | | | |
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| | | | | | and Writing Numbers) | in Reading and Writing Numbers) |
| | | | | <i>find the effect of dividing a one- or two-digit number by 10 and 100, identifying the value of the digits in the answer as units, tenths and hundredths</i> (copied from Fractions) | <i>recognise and use thousandths and relate them to tenths, hundredths and decimal equivalents</i> (copied from Fractions) | <i>identify the value of each digit to three decimal places and multiply and divide numbers by 10, 100 and 1000 where the answers are up to three decimal places</i> (copied from Fractions) |

| ROUNDING | | | | | |
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| Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
| | | | round any number to the nearest 10, 100 or 1 000 | round any number up to 1 000 000 to the nearest 10, 100, 1 000, 10 000 and 100 000 | round any whole number to a required degree of accuracy |
| | | | <i>round decimals with one decimal place to the nearest whole number</i> (copied from Fractions) | <i>round decimals with two decimal places to the nearest whole number and to one decimal place</i> (copied from Fractions) | <i>solve problems which require answers to be rounded to specified degrees of accuracy</i> (copied from Fractions) |
| PROBLEM SOLVING | | | | | |
| | use place value and number facts to solve problems | solve number problems and practical problems involving these ideas. | solve number and practical problems that involve all of the above and with increasingly large positive numbers | solve number problems and practical problems that involve all of the above | solve number and practical problems that involve all of the above |

| Reception | Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
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| Automatically recall number bonds for numbers 0–5 and some to 10 | represent and use number bonds and related subtraction facts within 20 | recall and use addition and subtraction facts to 20 fluently, and derive and use related facts up to 100 | | | | |
| MENTAL CALCULATION | | | | | | |
| Add and subtract 1 digit numbers to 10 including zero. | add and subtract one-digit and two-digit numbers to 20, including zero | add and subtract numbers using concrete objects, pictorial representations, and mentally, including: <ul style="list-style-type: none"> * a two-digit number and ones * a two-digit number and tens * two two-digit numbers * adding three one-digit numbers | add and subtract numbers mentally, including: <ul style="list-style-type: none"> * a three-digit number and ones * a three-digit number and tens * a three-digit number and hundreds | | add and subtract numbers mentally with increasingly large numbers | perform mental calculations, including with mixed operations and large numbers |
| Read, write and interpret mathematical statements involving addition (+), subtraction (-) and equals (=) signs (appears also in Written Methods) | read, write and interpret mathematical statements involving addition (+), subtraction (-) and equals (=) signs (appears also in Written Methods) | show that addition of two numbers can be done in any order (commutative) and subtraction of one number from another cannot | | | | use their knowledge of the order of operations to carry out calculations involving the four operations |

| WRITTEN METHODS | | | | | | |
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| Reception | Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
| Read, write and interpret mathematical statements involving addition (+), subtraction (-) and equals (=) signs (appears also in Written Methods) | read, write and interpret mathematical statements involving addition (+), subtraction (-) and equals (=) signs (appears also in Mental Calculation) | | add and subtract numbers with up to three digits, using formal written methods of columnar addition and subtraction | add and subtract numbers with up to 4 digits using the formal written methods of columnar addition and subtraction where appropriate | add and subtract whole numbers with more than 4 digits, including using formal written methods (columnar addition and subtraction) | |
| INVERSE OPERATIONS, ESTIMATING AND CHECKING ANSWERS | | | | | | |
| | | recognise and use the inverse relationship between addition and subtraction and use this to check calculations and solve missing number problems. | estimate the answer to a calculation and use inverse operations to check answers | estimate and use inverse operations to check answers to a calculation | use rounding to check answers to calculations and determine, in the context of a problem, levels of accuracy | use estimation to check answers to calculations and determine, in the context of a problem, levels of accuracy. |

| PROBLEM SOLVING | | | | | | |
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| Reception | Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
| solve one-step problems that involve addition and subtraction, using concrete objects and pictorial representations, such as there are 4 pieces of fruit and | solve one-step problems that involve addition and subtraction, using concrete objects and pictorial representations, and missing number problems such as $7 = \square - 9$ | solve problems with addition and subtraction: * using concrete objects and pictorial representations, including those involving numbers, quantities and measures | solve problems, including missing number problems, using number facts, place value, and more complex addition and subtraction | solve addition and subtraction two-step problems in contexts, deciding which operations and methods to use and why | solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why | solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why |

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| a bird eats 2, how many are left? | | * applying their increasing knowledge of mental and written methods | | | | |
| | | <i>solve simple problems in a practical context involving addition and subtraction of money of the same unit, including giving change (copied from Measurement)</i> | | | | Solve problems involving addition, subtraction, multiplication and division |

Progression in Multiplication and Division

| MULTIPLICATION & DIVISION FACTS | | | | | | |
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| Reception | Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
| <i>Count in twos and tens</i> | <i>count in multiples of twos, fives and tens (copied from Number and Place Value)</i> | <i>count in steps of 2, 3, and 5 from 0, and in tens from any number, forward or backward (copied from Number and Place Value)</i> | <i>count from 0 in multiples of 4, 8, 50 and 100 (copied from Number and Place Value)</i> | <i>count in multiples of 6, 7, 9, 25 and 1000 (copied from Number and Place Value)</i> | <i>count forwards or backwards in steps of powers of 10 for any given number up to 1 000 000 (copied from Number and Place Value)</i> | |
| | | recall and use multiplication and division facts for the 2, 5 and 10 multiplication tables, including recognising odd and even numbers | recall and use multiplication and division facts for the 3, 4 and 8 multiplication tables | recall multiplication and division facts for multiplication tables up to 12×12 | | |
| MENTAL CALCULATION | | | | | | |
| | | | write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, | use place value, known and derived facts to multiply and divide mentally, including: | multiply and divide numbers mentally drawing upon known facts | perform mental calculations, including with mixed operations and large numbers |

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| | | | including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods (appears also in Written Methods) | multiplying by 0 and 1; dividing by 1; multiplying together three numbers | | |
| | | show that multiplication of two numbers can be done in any order (commutative) and division of one number by another cannot | | recognise and use factor pairs and commutativity in mental calculations (appears also in Properties of Numbers) | multiply and divide whole numbers and those involving decimals by 10, 100 and 1000 | <i>associate a fraction with division and calculate decimal fraction equivalents (e.g. 0.375) for a simple fraction (e.g. $\frac{3}{8}$)</i> (copied from Fractions) |

WRITTEN CALCULATION

| Reception | Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
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| To divide a set of physical objects into even groups. | | calculate mathematical statements for multiplication and division within the multiplication tables and write them using the multiplication (\times), division (\div) and equals (=) signs | write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods (appears also in Mental Methods) | multiply two-digit and three-digit numbers by a one-digit number using formal written layout | multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-digit numbers | multiply multi-digit numbers up to 4 digits by a two-digit whole number using the formal written method of long multiplication |
| | | | | | divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret | divide numbers up to 4-digits by a two-digit whole number using the formal written method of short division where appropriate for the context divide numbers up to 4 digits by a two-digit whole number |

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| | | | | | remainders appropriately for the context | using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context |
| | | | | | | <i>use written division methods in cases where the answer has up to two decimal places (copied from Fractions (including decimals))</i> |

PROPERTIES OF NUMBERS: MULTIPLES, FACTORS, PRIMES, SQUARE AND CUBE NUMBERS

| Reception | Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
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| | | | | recognise and use factor pairs and commutativity in mental calculations (repeated) | <p>identify multiples and factors, including finding all factor pairs of a number, and common factors of two numbers.</p> <p>know and use the vocabulary of prime numbers, prime factors and composite (non-prime) numbers</p> <p>establish whether a number up to 100 is prime and recall prime numbers up to 19</p> | <p>identify common factors, common multiples and prime numbers</p> <p><i>use common factors to simplify fractions; use common multiples to express fractions in the same denomination (copied from Fractions)</i></p> |
| | | | | | recognise and use square numbers and cube numbers, and the notation for squared (2) and cubed (3) | <i>calculate, estimate and compare volume of cubes and cuboids using standard units, including centimetre cubed (cm^3) and cubic metres (m^3), and extending to other</i> |

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| | | | | | | units such as mm^3 and km^3 (copied from Measures) |
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| ORDER OF OPERATIONS | | | | | | |
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| Reception | Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
| | | | | | | use their knowledge of the order of operations to carry out calculations involving the four operations |
| INVERSE OPERATIONS, ESTIMATING AND CHECKING ANSWERS | | | | | | |
| | | | <i>estimate the answer to a calculation and use inverse operations to check answers</i> (copied from Addition and Subtraction) | <i>estimate and use inverse operations to check answers to a calculation</i> (copied from Addition and Subtraction) | | use estimation to check answers to calculations and determine, in the context of a problem, levels of accuracy |

| PROBLEM SOLVING | | | | | | |
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| Reception | Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
| | solve one-step problems involving multiplication and division, by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher | solve problems involving multiplication and division, using materials, arrays, repeated addition, mental methods, and multiplication and division facts, including problems in contexts | solve problems, including missing number problems, involving multiplication and division, including positive integer scaling problems and correspondence problems in which n objects are connected to m objects | solve problems involving multiplying and adding, including using the distributive law to multiply two digit numbers by one digit, integer scaling problems and harder correspondence problems such as n objects are connected to m objects | solve problems involving multiplication and division including using their knowledge of factors and multiples, squares and cubes | solve problems involving addition, subtraction, multiplication and division |
| | | | | | solve problems involving addition, subtraction, multiplication and division and a | |

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| | | | | | combination of these, including understanding the meaning of the equals sign | |
| | | | | | solve problems involving multiplication and division, including scaling by simple fractions and problems involving simple rates | <i>solve problems involving similar shapes where the scale factor is known or can be found</i> (copied from Ratio and Proportion) |

Progression in Fractions, Decimals and Percentages

| COUNTING IN FRACTIONAL STEPS | | | | | | |
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| Reception | Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
| | | <i>Pupils should count in fractions up to 10, starting from any number and using the 1/2 and 2/4 equivalence on the number line (Non Statutory Guidance)</i> | count up and down in tenths | count up and down in hundredths | | |
| RECOGNISING FRACTIONS | | | | | | |
| Recognise, find and name a half as one of two equal parts of an object, shape or quantity | recognise, find and name a half as one of two equal parts of an object, shape or quantity | recognise, find, name and write fractions $\frac{1}{3}$, $\frac{1}{4}$, $\frac{2}{4}$ and $\frac{3}{4}$ of a length, shape, set of objects or quantity | recognise, find and write fractions of a discrete set of objects: unit fractions and non-unit fractions with small denominators | recognise that hundredths arise when dividing an object by one hundred and dividing tenths by ten | recognise and use thousandths and relate them to tenths, hundredths and decimal equivalents (appears also in Equivalence) | |

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| | | | recognise that tenths arise from dividing an object into 10 equal parts and in dividing one – digit numbers or quantities by 10. | | | |
| | recognise, find and name a quarter as one of four equal parts of an object, shape or quantity | | recognise and use fractions as numbers: unit fractions and non-unit fractions with small denominators | | | |
| COMPARING FRACTIONS | | | | | | |
| | | | compare and order unit fractions, and fractions with the same denominators | | compare and order fractions whose denominators are all multiples of the same number | compare and order fractions, including fractions >1 |

| COMPARING DECIMALS | | | | | | |
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| Reception | Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
| | | | | compare numbers with the same number of decimal places up to two decimal places | read, write, order and compare numbers with up to three decimal places | identify the value of each digit in numbers given to three decimal places |
| ROUNDING INCLUDING DECIMALS | | | | | | |
| | | | | round decimals with one decimal place to the nearest whole number | round decimals with two decimal places to the nearest whole number and to one decimal place | solve problems which require answers to be rounded to specified degrees of accuracy |
| EQUIVALENCE (INCLUDING FRACTIONS, DECIMALS AND PERCENTAGES) | | | | | | |
| | | write simple fractions e.g. $\frac{1}{2}$ of 6 = 3 and recognise the | recognise and show, using diagrams, equivalent | recognise and show, using diagrams, families of common equivalent fractions | identify, name and write equivalent fractions of a given fraction, represented visually, including tenths and hundredths | use common factors to simplify fractions; use common multiples to express fractions in the |

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| | | equivalence of $\frac{2}{4}$ and $\frac{1}{2}$. | fractions with small denominators | | | same denomination |
| | | | | recognise and write decimal equivalents of any number of tenths or hundredths | read and write decimal numbers as fractions (e.g. $0.71 = \frac{71}{100}$) | associate a fraction with division and calculate decimal fraction equivalents (e.g. 0.375) for a simple fraction (e.g. $\frac{3}{8}$) |
| | | | | | recognise and use thousandths and relate them to tenths, hundredths and decimal equivalents | |
| | | | | recognise and write decimal equivalents to $\frac{1}{4}$; $\frac{1}{2}$; $\frac{3}{4}$ | recognise the per cent symbol (%) and understand that per cent relates to “number of parts per hundred”, and write percentages as a fraction with denominator 100 as a decimal fraction | recall and use equivalences between simple fractions, decimals and percentages, including in different contexts. |

ADDITION AND SUBTRACTION OF FRACTIONS

| Reception | Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
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| | | | add and subtract fractions with the same denominator within one whole (e.g. $\frac{5}{7} + \frac{1}{7} = \frac{6}{7}$) | add and subtract fractions with the same denominator | add and subtract fractions with the same denominator and multiples of the same number | add and subtract fractions with different denominators and mixed numbers, using the concept of equivalent fractions |
| | | | | | recognise mixed numbers and improper fractions and convert from one form to the other and write mathematical statements > 1 as a mixed number (e.g. $\frac{2}{5} + \frac{4}{5} = \frac{6}{5} = 1\frac{1}{5}$) | |

MULTIPLICATION AND DIVISION OF FRACTIONS

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| | | | | | multiply proper fractions and mixed numbers by whole numbers, supported by materials and diagrams | multiply simple pairs of proper fractions, writing the answer in its simplest form (e.g. $\frac{1}{4} \times \frac{1}{2} = \frac{1}{8}$) |
| | | | | | | multiply one-digit numbers with up to two decimal places by whole numbers |
| | | | | | | divide proper fractions by whole numbers (e.g. $\frac{1}{3} \div 2 = \frac{1}{6}$) |

MULTIPLICATION AND DIVISION OF DECIMALS

| Reception | Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
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| | | | | | | multiply one-digit numbers with up to two decimal places by whole numbers |
| | | | | find the effect of dividing a one- or two-digit number by 10 and 100, identifying the value of the digits in the answer as ones, tenths and hundredths | | multiply and divide numbers by 10, 100 and 1000 where the answers are up to three decimal places |
| | | | | | | identify the value of each digit to three decimal places and multiply and divide numbers by 10, 100 and 1000 where the answers are up to three |

| | | | | | | decimal places |
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| | | | | | | associate a fraction with division and calculate decimal fraction equivalents (e.g. 0.375) for a simple fraction (e.g. $\frac{3}{8}$) |
| | | | | | | use written division methods in cases where the answer has up to two decimal places |
| PROBLEM SOLVING | | | | | | |
| Reception | Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
| | | | solve problems that involve all of the above | solve problems involving increasingly harder fractions to calculate quantities, and fractions to divide quantities, including non-unit fractions where the answer is a whole number | solve problems involving numbers up to three decimal places | |
| | | | | solve simple measure and money problems involving fractions and decimals to two decimal places. | solve problems which require knowing percentage and decimal equivalents of $\frac{1}{2}$, $\frac{1}{4}$, $\frac{1}{5}$, $\frac{2}{5}$, $\frac{4}{5}$ and those with a denominator of a multiple of 10 or 25. | |

Progression in Algebra

| Algebra | | | | | | |
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| Reception | Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
| <p><i>Part-whole practical diagrams for composition/decomposition</i></p> <p>Explore the composition of numbers to 10.</p> | <p><i>solve one-step problems that involve addition and subtraction, using concrete objects and pictorial representations, and missing number problems such as $7 = \square - 9$ (copied from Addition and Subtraction)</i></p> | <p><i>recognise and use the inverse relationship between addition and subtraction and use this to check calculations and missing number problems. (copied from Addition and Subtraction)</i></p> | <p>solve problems, including missing number problems, using number facts, place value, and more complex addition and subtraction. (copied from Addition and Subtraction)</p> | | <p><i>use the properties of rectangles to deduce related facts and find missing lengths and angles (copied from Geometry: Properties of Shapes)</i></p> | <p>express missing number problems algebraically</p> |
| | | | <p><i>solve problems, including missing number problems, involving multiplication and division, including integer scaling (copied from Multiplication and Division)</i></p> | | | |
| | | <p><i>recall and use addition and subtraction facts to 20 fluently, and derive and use related facts up to 100 (copied from Addition and Subtraction)</i></p> | | | | <p>find pairs of numbers that satisfy number sentences involving two unknowns</p> |
| <p>Automatically recall number bonds for numbers 0–5 and some to 10</p> | <p><i>represent and use number bonds and related subtraction facts within 20 (copied from Addition and Subtraction)</i></p> | | | | | <p>enumerate all possibilities of combinations of two variables</p> |

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| Reception | Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
| | | | | <i>Perimeter can be expressed algebraically as $2(a + b)$ where a and b are the dimensions in the same unit. (Copied from NSG measurement)</i> | | use simple formulae |
| | | | | | | <i>recognise when it is possible to use formulae for area and volume of shapes (copied from Measurement)</i> |
| SEQUENCES | | | | | | |
| <i>Counting in twos Recognising before and after (Numbers and time) Days of the week First, next, after etc Morning, afternoon and evening</i> | <i>sequence events in chronological order using language such as: before and after, next, first, today, yesterday, tomorrow, morning, afternoon and evening (copied from Measurement)</i> | <i>compare and sequence intervals of time (copied from Measurement)</i> | | | | generate and describe linear number sequences |
| | | <i>order and arrange combinations of mathematical objects in patterns (copied from Geometry: position and direction)</i> | | | | |

Progression in Ratio and Proportion

| Statements only appear in Year 6 but should be connected to previous learning, particularly fractions and multiplication and division | | | | | |
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| | | | | | Year 6 |
| | | | | | solve problems involving the relative sizes of two quantities where missing |

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| | | | | | values can be found by using integer multiplication and division facts |
| | | | | | solve problems involving the calculation of percentages [for example, of measures, and such as 15% of 360] and the use of percentages for comparison |
| | | | | | solve problems involving similar shapes where the scale factor is known or can be found |
| | | | | | solve problems involving unequal sharing and grouping using knowledge of fractions and multiples. |

Progression in Measurement

| Reception | Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
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| <p>Compare length, weight and capacity</p> <p>Use comparative language using 'than' and encourage children to use this vocabulary. For example: "This is heavier than that." Ask children to make and test predictions. "What if we pour the jugful into the</p> | <p>compare, describe and solve practical problems for:</p> <ul style="list-style-type: none"> * lengths and heights [e.g. long/short, longer/shorter, tall/short, double/half] * mass/weight [e.g. heavy/light, | <p>compare and order lengths, mass, volume/capacity and record the results using $>$, $<$ and $=$</p> | | <p>estimate, compare and calculate different measures, including money in pounds and pence (also included in Measuring)</p> | <p>calculate and compare the area of squares and rectangles including using standard units, square centimetres (cm^2) and square metres (m^2) and estimate the area of irregular</p> | <p>calculate, estimate and compare volume of cubes and cuboids using standard units, including centimetre cubed (cm^3) and cubic metres (m^3), and</p> |

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| teapot? Which holds more?" | <p>heavier than, lighter than]</p> <p>* capacity and volume [e.g. full/empty, more than, less than, half, half full, quarter]</p> <p>* time [e.g. quicker, slower, earlier, later]</p> | | | | <p>shapes (also included in measuring)</p> <hr/> <p>estimate volume (e.g. using 1 cm³ blocks to build cubes and cuboids) and capacity (e.g. using water)</p> | extending to other units such as mm ³ and km ³ . |
| Days of the week Chronological order Times of the day | sequence events in chronological order using language [e.g. before and after, next, first, today, yesterday, tomorrow, morning, afternoon and evening] | compare and sequence intervals of time | compare durations of events, for example to calculate the time taken by particular events or tasks | | | |
| | | | estimate and read time with increasing accuracy to the nearest minute; record and compare time in terms of seconds, minutes, hours and o'clock; use vocabulary such as a.m./p.m., morning, afternoon, noon and midnight (appears also in Telling the Time) | | | |

| MEASURING and CALCULATING | | | | | | |
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| Reception | Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
| Use non-standard units to measure * lengths and heights * mass/weight * capacity and volume * time | measure and begin to record the following: * lengths and heights * mass/weight * capacity and volume * time (hours, minutes, seconds) | choose and use appropriate standard units to estimate and measure length/height in any direction (m/cm); mass (kg/g); temperature (°C); capacity (litres/ml) to the nearest appropriate unit, using rulers, scales, thermometers and measuring vessels | measure, compare, add and subtract: lengths (m/cm/mm); mass (kg/g); volume/capacity (l/ml) | estimate, compare and calculate different measures , including money in pounds and pence (appears also in Comparing) | use all four operations to solve problems involving measure (e.g. length, mass, volume, money) using decimal notation including scaling. | solve problems involving the calculation and conversion of units of measure , using decimal notation up to three decimal places where appropriate (appears also in Converting) |
| | | | measure the perimeter of simple 2-D shapes | measure and calculate the perimeter of a rectilinear figure (including squares) in centimetres and metres | measure and calculate the perimeter of composite rectilinear shapes in centimetres and metres | recognise that shapes with the same areas can have different perimeters and vice versa |

| MEASURING and CALCULATING | | | | | | |
|---------------------------|-----------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------|--------|--------|--------|
| Reception | Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
| Recognise 1p coins. | recognise and know the value of different denominations of coins and notes | recognise and use symbols for pounds (£) and pence (p); combine amounts to make a particular value | add and subtract amounts of money to give change, using both £ and p in practical contexts | | | |
| | | find different combinations of coins that equal the same amounts of money | | | | |

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| | | solve simple problems in a practical context involving addition and subtraction of money of the same unit, including giving change | | | | |
| | | | | find the area of rectilinear shapes by counting squares | calculate and compare the area of squares and rectangles including using standard units, square centimetres (cm ²) and square metres (m ²) and estimate the area of irregular shapes | calculate the area of parallelograms and triangles |
| | | | | | <i>recognise and use square numbers and cube numbers, and the notation for squared (²) and cubed (³)</i> (copied from Multiplication and Division) | calculate, estimate and compare volume of cubes and cuboids using standard units, including cubic centimetres (cm ³) and cubic metres (m ³), and extending to other units [e.g. mm ³ and km ³]. |
| | | | | | | recognise when it is possible to use formulae for area and volume of shapes |

TELLING THE TIME

| Reception | Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
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| Tell the time to the hour | tell the time to the hour and half past the hour and draw the hands on a clock face to show these times. | tell and write the time to five minutes, including quarter past/to the hour and draw the hands on a clock face to show these times. | tell and write the time from an analogue clock, including using Roman numerals from I to XII, and 12-hour and 24-hour clocks | read, write and convert time between analogue and digital 12 and 24-hour clocks (appears also in Converting) | | |
| Times of the day Days of the week | recognise and use language relating to dates, including days of the week, weeks, | know the number of minutes in an hour and the number of hours in a day. | estimate and read time with increasing accuracy to the nearest minute; record and | | | |

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| | months and years | (appears also in Converting) | compare time in terms of seconds, minutes, hours and o'clock; use vocabulary such as a.m./p.m., morning, afternoon, noon and midnight (appears also in Comparing and Estimating) | | | |
| | | | | solve problems involving converting from hours to minutes; minutes to seconds; years to months; weeks to days (appears also in Converting) | solve problems involving converting between units of time | |

Progression in Properties of shapes

| Properties of Shapes | | | | | | |
|----------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------|--------|------------------------------------------------------------------------------|----------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------|
| Reception | Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
| | recognise and name common 2-D and 3-D shapes, including: * 2-D shapes [e.g. rectangles (including squares), circles and triangles] * 3-D shapes [e.g. cuboids (including cubes), pyramids and spheres]. | identify and describe the properties of 2-D shapes, including the number of sides and line symmetry in a vertical line | | identify lines of symmetry in 2-D shapes presented in different orientations | identify 3-D shapes, including cubes and other cuboids, from 2-D representations | recognise, describe and build simple 3-D shapes, including making nets (appears also in Drawing and Constructing) |
| | | identify and describe the properties of 3-D shapes, including the number of edges, vertices and faces | | | | illustrate and name parts of circles, including radius, diameter and circumference and |

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| | | | | | | know that the diameter is twice the radius |
| | | identify 2-D shapes on the surface of 3-D shapes, [for example, a circle on a cylinder and a triangle on a pyramid] | | | | |

DRAWING AND CONSTRUCTING

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| | | | draw 2-D shapes and make 3-D shapes using modelling materials; recognise 3-D shapes in different orientations and describe them | complete a simple symmetric figure with respect to a specific line of symmetry | draw given angles, and measure them in degrees ($^{\circ}$) | draw 2-D shapes using given dimensions and angles |
| | | | | | | recognise, describe and build simple 3-D shapes, including making nets (appears also in Identifying Shapes and Their Properties) |

COMPARING AND CLASSIFYING

| Reception | Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
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| | | compare and sort common 2-D and 3-D shapes and everyday objects | | compare and classify geometric shapes, including quadrilaterals and triangles, based on their properties and sizes | use the properties of rectangles to deduce related facts and find missing lengths and angles | compare and classify geometric shapes based on their properties and sizes and find unknown angles in any triangles, quadrilaterals, and |

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| | | | | | distinguish between regular and irregular polygons based on reasoning about equal sides and angles | regular polygons |
| ANGLES | | | | | | |
| | | | recognise angles as a property of shape or a description of a turn | | know angles are measured in degrees: estimate and compare acute, obtuse and reflex angles | |
| | | | identify right angles, recognise that two right angles make a half-turn, three make three quarters of a turn and four a complete turn; identify whether angles are greater than or less than a right angle | identify acute and obtuse angles and compare and order angles up to two right angles by size | identify: * angles at a point and one whole turn (total 360°) * angles at a point on a straight line and $\frac{1}{2}$ a turn (total 180°) * other multiples of 90° | recognise angles where they meet at a point, are on a straight line, or are vertically opposite, and find missing angles |
| | | | identify horizontal and vertical lines and pairs of perpendicular and parallel lines | | | |

Progression in Position, Direction and Movement

| POSITION, DIRECTION AND MOVEMENT | | | | | | |
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| Reception | Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
| | describe position, direction and movement, including half, quarter and | use mathematical vocabulary to describe position, direction and movement including | | describe positions on a 2-D grid as coordinates in the first quadrant | identify, describe and represent the position of a shape following a reflection or | describe positions on the full coordinate grid (all four quadrants) |

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| | three-quarter turns. | movement in a straight line and distinguishing between rotation as a turn and in terms of right angles for quarter, half and three-quarter turns (clockwise and anti-clockwise) | | describe movements between positions as translations of a given unit to the left/right and up/down | translation, using the appropriate language, and know that the shape has not changed | draw and translate simple shapes on the coordinate plane, and reflect them in the axes. |
| | | | | plot specified points and draw sides to complete a given polygon | | |
| PATTERN | | | | | | |
| | | order and arrange combinations of mathematical objects in patterns and sequences | | | | |

Progression in Statistics

| STATISTICS - INTERPRETING, CONSTRUCTING AND PRESENTING DATA | | | | | | |
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| Reception | Year 1 | Year 2 | Year 3 | Year 4 | Year 5 | Year 6 |
| | | interpret and construct simple pictograms, tally charts, block diagrams and simple tables | interpret and present data using bar charts, pictograms and tables | interpret and present discrete and continuous data using appropriate graphical methods, including bar charts and time graphs | complete, read and interpret information in tables, including timetables | interpret and construct pie charts and line graphs and use these to solve problems |
| | | ask and answer simple questions by counting the number of objects in each category and | | | | |

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| | | sorting the categories by quantity | | | | |
| | | ask and answer questions about totalling and comparing categorical data | | | | |
| SOLVING PROBLEMS | | | | | | |
| | | | solve one-step and two-step questions [e.g. 'How many more?' and 'How many fewer?'] using information presented in scaled bar charts and pictograms and tables. | solve comparison, sum and difference problems using information presented in bar charts, pictograms, tables and other graphs. | solve comparison, sum and difference problems using information presented in a line graph | calculate and interpret the mean as an average |